

line element of Stiles
(1946) with „color values“ P, D, T
three separate color signal functions

$$F(P) = i \ln(1+9P) \\ F(D) = j \ln(1+9D) \\ F(T) = k \ln(1+9T)$$

Taylor-derivations:

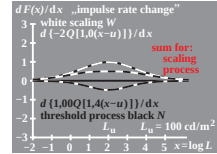
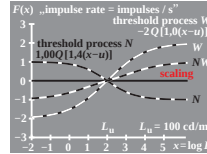
$$\Delta F(P, D, T) = \frac{dF}{dP} \Delta P + \frac{dF}{dD} \Delta D + \frac{dF}{dT} \Delta T \\ = -\frac{9i}{1+9P} \Delta P + \frac{9j}{1+9D} \Delta D + \frac{9k}{1+9T} \Delta T$$

line element of Vos & Walraven
(1972) with „color values“ P, D, T
three separate color signal functions

$$F(P) = -2i\sqrt{P} \\ F(D) = -2j\sqrt{D} \\ F(T) = -2k\sqrt{T}$$

Taylor-derivations:

$$\Delta F(P, D, T) = \frac{dF}{dP} \Delta P + \frac{dF}{dD} \Delta D + \frac{dF}{dT} \Delta T \\ \Delta F(P, D, T) = \frac{-i}{\sqrt{P}} \Delta P + \frac{-j}{\sqrt{D}} \Delta D + \frac{-k}{\sqrt{T}} \Delta T$$



functions $q[k(x-u)]$
„achromatic signal“-description

with $x = \log L$ (L = luminance)
 $u = \log L_u$ (L_u = surround luminance)

$$q[k(x-u)] = 1 + 1/[1 + \sqrt{2}e^{k(x-u)}] \\ \text{function values:}$$

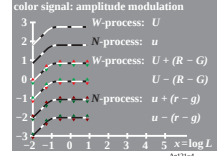
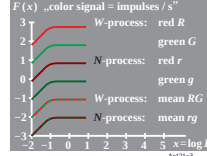
$$q[k(x-u) \rightarrow +\infty] = 1 \\ q[k(x-u) = 0] = \sqrt{2} \\ q[k(x-u) \rightarrow -\infty] = 2$$

„achromatic signal“-description
functions $Q_{lm}[k(x-u)]$

with $x = \log L$ (L = luminance)
 $u = \log L_u$ (L_u = surround luminance)

$$Q_{lm}[k(x-u)] = \frac{1}{\ln 2} \ln q[k(x-u)] - m \\ \text{function values with } l = m = 1:$$

$$Q[k(x-u) \rightarrow +\infty] = 1 \\ Q[k(x-u) = 0] = 0 \\ Q[k(x-u) \rightarrow -\infty] = -1$$



„achromatic signal“-discrimination
as function of relative light density
 $h = \ln H = k(x-u)$ $\ln$ = natural log.

$$Q' = \frac{dQ}{dh} = \frac{dQ}{d[\ln\{1 + 1/(1 + \sqrt{2}e^h)\}]} / \ln 2 \\ = -\sqrt{2} / [\ln 2(1 + \sqrt{2}H)(2 + \sqrt{2}H)]$$

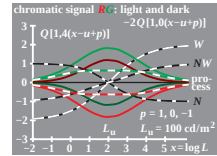
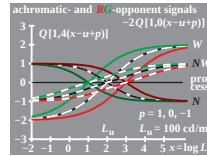
function values:

$$Q'[k(x-u) \rightarrow +\infty] = 0 \\ Q'[k(x-u) = 0] = -0,5 \\ Q'[k(x-u) \rightarrow -\infty] = 0$$

luminance discrimination
possibility $L/\Delta L$ as function of H

$$\text{with: } L = 10^8 H = e^h = 10^{\ln 8 + k(x-u)} \\ dL/dx = \ln 10 L \quad dH/dx = k H \\ \text{it follows: } L/\Delta L = [kH/(dH \ln 10)] \\ \frac{dL}{L} = \text{const } H / [(1 + \sqrt{2}H)(2 + \sqrt{2}H)]$$

$$Q'[k(x-u) \rightarrow +\infty] = 0 \\ Q'[k(x-u) = 0] = \text{maximum} \\ Q'[k(x-u) \rightarrow -\infty] = 0$$



double line element of Richter
(1987) for the lighting technic with
luminance $L = F(P, D, T)$

$$\text{luminance signal function } F(L) \\ F(L) = iQ(H) = \begin{cases} iQ(\bar{H}) & (x < u) \\ iQ(\bar{H}) & (x \geq u) \end{cases}$$

$$\text{with: } k=1,4 \quad k=1 \quad i=1 \quad i=-2 \\ x = \log L \quad u = \log L_u \\ H = e^{k(x-u)}, \bar{H} = e^{k(x-u)}, \bar{H} = e^{k(x-u)}$$

double line element of Richter
(1987) for the lighting technic with
luminance $L = F(P, D, T)$

$$\text{luminance signal function } F(L) \\ F(L) = iQ(H) \quad H = e^{k(x-u)} \\ Q[\ln\{1 + 1/(1 + \sqrt{2}H)\}]/\ln 2 - 1$$

Taylor-derivations:

$$\Delta F(L) = \frac{dF}{dL} \Delta L = i \frac{dQ}{dH} \Delta H \\ = -i\sqrt{2} \Delta H / [\ln 2(1 + \sqrt{2}H)(2 + \sqrt{2}H)]$$

