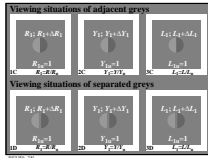
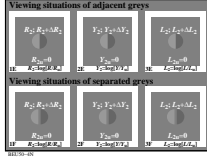
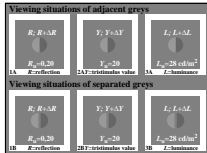


sensation scaling functions
lightness L^* and tristimulus value Y
adaptation on surround white Y
 $L^*_w = 100 (Y / 100)^{1/2,0}$
adaptation on surround grey Z
 $L^*_Z = 100 (Y / 100)^{1/2,4}$
description with CIE LAB 1976
 $L^*_{CIE LAB} = 116 (Y / 100)^{1/3,0} - 16$
adaptation on surround black N
 $L^*_N = 100 (Y / 100)^{1/3,0}$



Lightness L^*_Z for surround mean grey Z (sRGB)
For separated surface colours in the range 0.0036- $R<0,90$
or the digital range 1/255-0.0039- $R<1,00$ it is valid:
 $L^*_Z = a (R/R_w)^b$ [1] $a=100; R_w=1,00; b=0,42-1/2,4$
 $= b (R/R_w)^b$ [2] $b=a/R_w^{b-50}; R_w=0,18$
For $R=R_w$ it is valid: $L^*_Z=a=50$.
Derivation of equation [2] gives with $1-k=0,58$:
 $\delta(L^*_Z)/\delta R = c (R/R_w)^{b-1}$ [3] $c = (b \cdot k) R_w = 21/18 = 1,17$
or for the threshold $\delta(L^*_Z)=1$
 $\delta R = d (R/R_w)^{b-1}$ [4] $d = Y_w/b(k) = 18/21 = 0,86$
For the surround lightness $L^*_{ZPN}=50$ with $R=R_w$ the threshold is
 $\delta R_{PN}=0,86$. This threshold is independent of k .

Lightness L^*_Z for surround mean grey Z (sRGB)
For separated surface colours in the range 3,6- $T<90$
or the digital range 100/255-0,39- $T<100$ it is valid:
 $L^*_Z = a (T/T_w)^b$ [1] $a=100; T_w=100; b=0,42-1/2,4$
 $= b (T/T_w)^b$ [2] $b=a/T_w^{b-50}; T_w=18$
For $T=T_w$ it is valid: $L^*_Z=a=50$.
Derivation of equation [2] gives with $1-k=0,58$:
 $\delta(L^*_Z)/\delta T = c (T/T_w)^{b-1}$ [3] $c = (b \cdot k) T_w = 21/18 = 1,17$
or for the threshold $\delta(L^*_Z)=1$
 $\delta T = d (T/T_w)^{b-1}$ [4] $d = Y_w/b(k) = 18/21 = 0,86$
For the surround lightness $L^*_{ZPN}=50$ with $T=T_w$ the threshold is
 $\delta T_{PN}=0,86$. This threshold is independent of k .



Lightness L^*_{PN} for the Just Noticeable Difference (JND)
For adjacent surface colours in the range 0.0036- $R<0,90$
or the digital range 1/255-0.0039- $R<1,00$ it is valid:
 $L^*_{PN} = a (R/R_w)^b$ [1] $a=572; R_w=1,00; b=0,14-1/2,2$
 $= b (R/R_w)^b$ [2] $b=a/R_w^{b-450}; R_w=0,18$
For $R=R_w$ it is valid: $L^*_{PN}=450$.
Derivation of equation [2] gives with $1-k=0,86$:
 $\delta(L^*_{PN})/\delta R = c (R/R_w)^{b-1}$ [3] $c = (b \cdot k) R_w = 63/18 = 3,5$
or for the threshold $\delta(L^*_{PN})=1$
 $\delta R = d (R/R_w)^{b-1}$ [4] $d = Y_w/b(k) = 18/63 = 0,29$
For the surround lightness $L^*_{PNPN}=450$ with $R=R_w$ the threshold is
 $\delta R_{PNPN}=0,29$. This threshold is independent of k .

Lightness L^*_{PN} for the Just Noticeable Difference (JND)
For adjacent surface colours in the range 3,6- $T<90$
or the digital range 100/255-0,39- $T<100$ it is valid:
 $L^*_{PN} = a (T/T_w)^b$ [1] $a=572; T_w=100; b=0,14-1/2,2$
 $= b (T/T_w)^b$ [2] $b=a/T_w^{b-450}; T_w=18$
For $T=T_w$ it is valid: $L^*_{PN}=450$.
Derivation of equation [2] gives with $1-k=0,86$:
 $\delta(L^*_{PN})/\delta T = c (T/T_w)^{b-1}$ [3] $c = (b \cdot k) T_w = 63/18 = 3,5$
or for the threshold $\delta(L^*_{PN})=1$
 $\delta T = d (T/T_w)^{b-1}$ [4] $d = Y_w/b(k) = 18/63 = 0,29$
For the surround lightness $L^*_{PNPN}=450$ with $T=T_w$ the threshold is
 $\delta T_{PNPN}=0,29$. This threshold is independent of k .

Lightness L^*_Z for surround mean grey Z (sRGB)
For separated surface colours in the range 3,6- $L<90$
or the digital range 100/255-0,39- $L<100$ it is valid:
 $L^*_Z = a (L/L_w)^b$ [1] $a=100; L_w=142; d/m^2; b=0,42-1/2,4$
 $= b (L/L_w)^b$ [2] $b=a/L_w^{b-50}; L_w=18$
For $L=L_w$ it is valid: $L^*_Z=a=50$.
Derivation of equation [2] gives with $1-k=0,58$:
 $\delta(L^*_Z)/\delta L = c (L/L_w)^{b-1}$ [3] $c = (b \cdot k) L_w = 21/18 = 1,17$
or for the threshold $\delta(L^*_Z)=1$
 $\delta L = d (L/L_w)^{b-1}$ [4] $d = L_w/b(k) = 18/21 = 0,86$
For the surround lightness $L^*_{ZPN}=50$ with $L=L_w$ the threshold is
 $\delta L_{PN}=0,86$. This threshold is independent of k .

Lightness L^*_N for surround black N
For separated surface colours in the range 0.0036- $R<0,90$
or the digital range 1/255-0.0039- $R<1,00$ it is valid:
 $L^*_N = a (R/R_w)^b$ [1] $a=100; R_w=1,00; b=0,33-1/3,0$
 $= b (R/R_w)^b$ [2] $b=a/R_w^{b-56}; R_w=0,18$
For $R=R_w$ it is valid: $L^*_N=a=56$.
Derivation of equation [2] gives with $1-k=0,67$:
 $\delta(L^*_N)/\delta R = c (R/R_w)^{b-1}$ [3] $c = (b \cdot k) R_w = 19/18 = 1,05$
or for the threshold $\delta(L^*_N)=1$
 $\delta R = d (R/R_w)^{b-1}$ [4] $d = R_w/b(k) = 18/19 = 0,95$
For the surround lightness $L^*_{NPN}=50$ with $R=R_w$ the threshold is
 $\delta R_{PN}=0,95$. This threshold is independent of k .

Lightness L^*_N for surround black N
For adjacent surface colours in the range 3,6- $T<90$
or the digital range 100/255-0,39- $T<100$ it is valid:
 $L^*_N = a (T/T_w)^b$ [1] $a=100; T_w=100; b=0,33-1/3,0$
 $= b (T/T_w)^b$ [2] $b=a/T_w^{b-56}; T_w=18$
For $T=T_w$ it is valid: $L^*_N=a=56$.
Derivation of equation [2] gives with $1-k=0,67$:
 $\delta(L^*_N)/\delta T = c (T/T_w)^{b-1}$ [3] $c = (b \cdot k) T_w = 19/18 = 1,05$
or for the threshold $\delta(L^*_N)=1$
 $\delta T = d (T/T_w)^{b-1}$ [4] $d = T_w/b(k) = 18/19 = 0,95$
For the surround lightness $L^*_{NPN}=50$ with $T=T_w$ the threshold is
 $\delta T_{PN}=0,95$. This threshold is independent of k .

Lightness L^*_N for surround black N
For adjacent surface colours in the range 3,6- $L<90$
or the digital range 100/255-0,39- $L<100$ it is valid:
 $L^*_N = a (L/L_w)^b$ [1] $a=100; L_w=142; d/m^2; b=0,33-1/3,0$
 $= b (L/L_w)^b$ [2] $b=a/L_w^{b-56}; L_w=18$
For $L=L_w$ it is valid: $L^*_N=a=56$.
Derivation of equation [2] gives with $1-k=0,67$:
 $\delta(L^*_N)/\delta L = c (L/L_w)^{b-1}$ [3] $c = (b \cdot k) L_w = 19/18 = 1,05$
or for the threshold $\delta(L^*_N)=1$
 $\delta L = d (L/L_w)^{b-1}$ [4] $d = L_w/b(k) = 18/19 = 0,95$
For the surround lightness $L^*_{NPN}=50$ with $L=L_w$ the threshold is
 $\delta L_{PN}=0,95$. This threshold is independent of k .

Lightness L^*_{PN} for the Just Noticeable Difference (JND)
For adjacent surface colours in the range 3,6- $L<90$
or the digital range 100/255-0,39- $L<100$ it is valid:
 $L^*_{PN} = a (L/L_w)^b$ [1] $a=572; L_w=142; d/m^2; b=0,14-1/2,2$
 $= b (L/L_w)^b$ [2] $b=a/L_w^{b-450}; L_w=18$
For $L=L_w$ it is valid: $L^*_{PN}=450$.
Derivation of equation [2] gives with $1-k=0,86$:
 $\delta(L^*_{PN})/\delta L = c (L/L_w)^{b-1}$ [3] $c = (b \cdot k) L_w = 63/18 = 3,5$
or for the threshold $\delta(L^*_{PN})=1$
 $\delta L = d (L/L_w)^{b-1}$ [4] $d = L_w/b(k) = 18/63 = 0,29$
For the surround lightness $L^*_{PNPN}=450$ with $L=L_w$ the threshold is
 $\delta L_{PNPN}=0,29$. This threshold is independent of k .

Lightness L^*_w for surround white W
For separated surface colours in the range 0.0036- $R<0,90$
or the digital range 1/255-0.0039- $R<1,00$ it is valid:
 $L^*_w = a (R/R_w)^b$ [1] $a=100; R_w=1,00; b=0,50-1/2,0$
 $= b (R/R_w)^b$ [2] $b=a/R_w^{b-42}; R_w=0,18$
For $R=R_w$ it is valid: $L^*_w=a=42$.
Derivation of equation [2] gives with $1-k=0,50$:
 $\delta(L^*_w)/\delta R = c (R/R_w)^{b-1}$ [3] $c = (b \cdot k) R_w = 21/18 = 1,17$
or for the threshold $\delta(L^*_w)=1$
 $\delta R = d (R/R_w)^{b-1}$ [4] $d = R_w/b(k) = 18/21 = 0,86$
For the surround lightness $L^*_{wPN}=50$ with $R=R_w$ the threshold is
 $\delta R_{PN}=0,86$. This threshold is independent of k .

Lightness L^*_w for surround white W
For adjacent surface colours in the range 3,6- $T<90$
or the digital range 100/255-0,39- $T<100$ it is valid:
 $L^*_w = a (T/T_w)^b$ [1] $a=100; T_w=100; b=0,50-1/2,0$
 $= b (T/T_w)^b$ [2] $b=a/T_w^{b-42}; T_w=18$
For $T=T_w$ it is valid: $L^*_w=a=42$.
Derivation of equation [2] gives with $1-k=0,50$:
 $\delta(L^*_w)/\delta T = c (T/T_w)^{b-1}$ [3] $c = (b \cdot k) T_w = 21/18 = 1,17$
or for the threshold $\delta(L^*_w)=1$
 $\delta T = d (T/T_w)^{b-1}$ [4] $d = T_w/b(k) = 18/21 = 0,86$
For the surround lightness $L^*_{wPN}=50$ with $T=T_w$ the threshold is
 $\delta T_{PN}=0,86$. This threshold is independent of k .

Lightness L^*_w for surround white W
For adjacent surface colours in the range 3,6- $L<90$
or the digital range 100/255-0,39- $L<100$ it is valid:
 $L^*_w = a (L/L_w)^b$ [1] $a=100; L_w=142; d/m^2; b=0,50-1/2,0$
 $= b (L/L_w)^b$ [2] $b=a/L_w^{b-42}; L_w=18$
For $L=L_w$ it is valid: $L^*_w=a=42$.
Derivation of equation [2] gives with $1-k=0,50$:
 $\delta(L^*_w)/\delta L = c (L/L_w)^{b-1}$ [3] $c = (b \cdot k) L_w = 21/18 = 1,17$
or for the threshold $\delta(L^*_w)=1$
 $\delta L = d (L/L_w)^{b-1}$ [4] $d = L_w/b(k) = 18/21 = 0,86$
For the surround lightness $L^*_{wPN}=50$ with $L=L_w$ the threshold is
 $\delta L_{PN}=0,86$. This threshold is independent of k .