

## Transformation between the Judd tristimulus and opponent values

Data see K. Richter, PhD thesis, University of Basel (Switzerland), 1969, page 81.

For the antagonistic spectral elementary colours

$\lambda_B = 475 \text{ nm}$ ,  $\lambda_G = 502 \text{ nm}$ ,  $\lambda_Y = 574 \text{ nm}$ ,  $\lambda_R = 494 \text{ nm}$

modern coordinates  $\bar{l}$ ,  $\bar{a}$ ,  $\bar{b}$  are used instead of  $\bar{x}_i$  ( $i=1$  to 3).

Linear model equations between spectral colour values in both directions:

$$\begin{pmatrix} \bar{l}(\lambda) \\ \bar{a}(\lambda) \\ \bar{b}(\lambda) \end{pmatrix} = \begin{pmatrix} b_{11} & b_{12} & b_{13} \\ b_{21} & b_{22} & b_{23} \\ b_{31} & b_{32} & b_{33} \end{pmatrix} \cdot \begin{pmatrix} \bar{x}(\lambda) \\ \bar{y}(\lambda) \\ \bar{z}(\lambda) \end{pmatrix} = \begin{pmatrix} 0,0000 & 1,0000 & 0,0000 \\ 2,9797 & -2,6662 & -0,0960 \\ -0,4139 & 1,4571 & -2,4046 \end{pmatrix} \cdot \begin{pmatrix} \bar{x}(\lambda) \\ \bar{y}(\lambda) \\ \bar{z}(\lambda) \end{pmatrix} \quad (1)$$

$$\begin{pmatrix} \bar{x}(\lambda) \\ \bar{y}(\lambda) \\ \bar{z}(\lambda) \end{pmatrix} = \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} \cdot \begin{pmatrix} \bar{l}(\lambda) \\ \bar{a}(\lambda) \\ \bar{b}(\lambda) \end{pmatrix} = \begin{pmatrix} 0,9093 & 0,3338 & -0,0133 \\ 1,0000 & 0,0000 & 0,0000 \\ 0,4494 & -0,0574 & -0,4136 \end{pmatrix} \cdot \begin{pmatrix} \bar{l}(\lambda) \\ \bar{a}(\lambda) \\ \bar{b}(\lambda) \end{pmatrix} \quad (2)$$

The tristimulus values  $L$ ,  $A$ ,  $B$  and  $X$ ,  $Y$ ,  $Z$  need the same transformations.

The unnormalized purity data  $a_u$  and  $b_u$  are defined in LabMUN 1969 as follows:

$$a_u = X/Y = x/y \quad (3) \qquad b_u = -Z/Y = -z/y \quad (4) \qquad z = 1 - x - y \quad (5)$$

The purity data  $a_u$  and  $b_u$  are defined in LabMUN 1969 as follows:

$$\begin{aligned} a_u &= [(b_{21} - b_{23})x + (b_{22} - b_{23})y + b_{23}] / y \\ &= (3,0757x - 2,5702y - 0,0960) / y \end{aligned} \quad (6)$$

$$\begin{aligned} b_u &= [(b_{31} - b_{33})x + (b_{32} - b_{33})y + b_{33}] / y \\ &= (1,9906x + 3,8617y - 2,4046) / y \end{aligned} \quad (7)$$