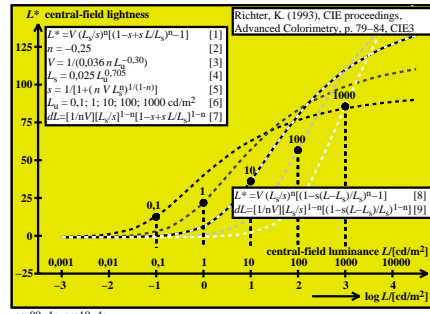
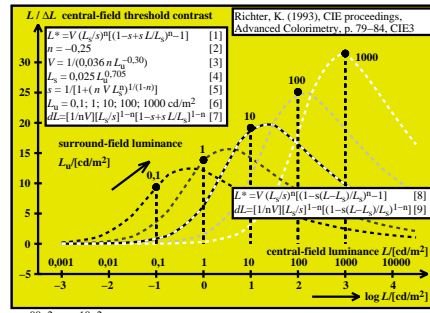


Line-element equations according to CIE 230:2019
 Colour-threshold (t) function $f_t(x) = \Delta Y_t = \Delta x Y_u$ (0)
 $\Delta Y_t = (A_1 + A_2 Y) / A_0$ $A_0 = 1,5$, $A_1 = 0,0170$, $A_2 = 0,0058$
 $f_{tu}(x) = \frac{\Delta Y_t}{\Delta Y_{tu}} = \frac{1+b \cdot x}{1+b}$ $b = A_2 Y_u / A_1$ $x = Y / Y_u$ (1)
 $F_{tu}(x) = \int \frac{f_t(tu(x))}{f_{tu}(x)} dx = \int \frac{b}{1+b \cdot x} dx$ (2)
 Example for $L^*_{tu}(x)$, ΔY_t with $x = Y/Y_u$, $x_0 = 1$, $b = 6,141$:
 $L^*_{tu}(x) = \frac{L^*_{tu}(x)}{L^*_{tu}(x)} = \frac{\ln(1+b \cdot x)}{\ln(1+b)}$ (3)
 $f_{tu}(x) = \frac{\Delta Y_t}{\Delta Y_{tu}} = \frac{1+b \cdot x}{1+b}$ (4)

Line-element equations: lightness – luminance¹⁾
 Simple equation by the **Weber-Fechner law** between the lightness L^* and the luminance L
 $\frac{\Delta L^*}{L^*} = n \frac{\Delta L}{L}$ (1)
 It is assumed that the luminance threshold L_s
 $\frac{\Delta L^*}{L^* + L_s} = n \frac{\Delta L}{L + L_s}$ (2)
 Integration on both sides and requirement $L^* = 0$ for $L = 0$
 $L^* = L^*_s [(1 + \frac{L}{L_s})^n - 1]$ (3)
 Small change with threshold factor s and $L^* = 0$ for $L = L_s$
 $L^* = L^*_s [(1 + s \frac{L-L_s}{L_s})^n - 1]$ (4)

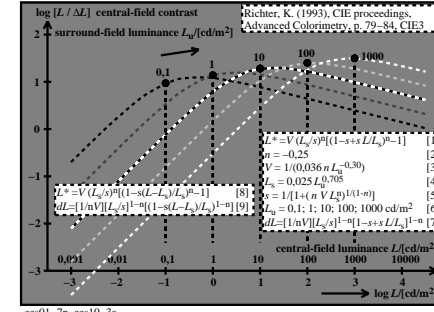
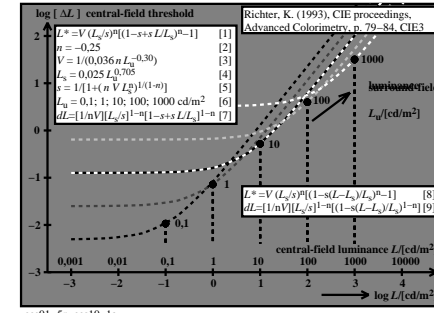
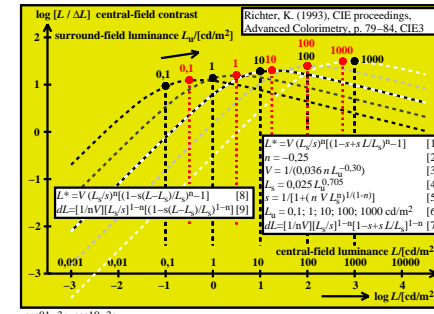
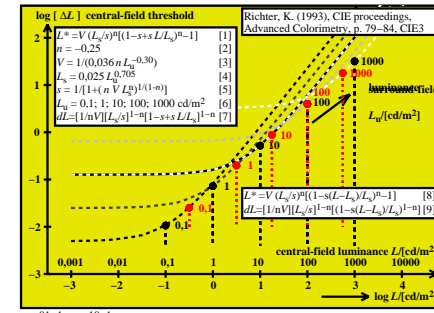
1) Richter, Klaus, (1969), Antagonistic signals in colour vision and relation with the perceived colour order (in German), Dis. Universität Basel, 150 pages, see 115-123, ces00-7N
 2) Newhall, S.M., Nickerson, D., Judd, D.B. (1943), Final report of the O.S.A. subcommittee on the spacing of Munsell Colors, GSA 33, 383-418, see p. 417
 3) ISO/CIE 11664-4:2019 Colorimetry, CIE 1976 $L^*a^*b^*$ colour space
 ces00-8N



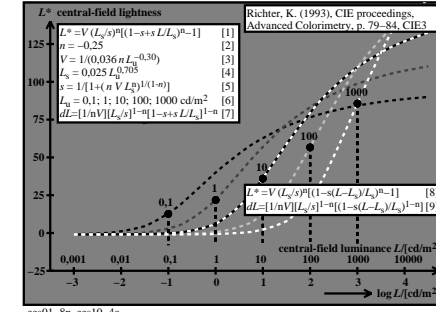
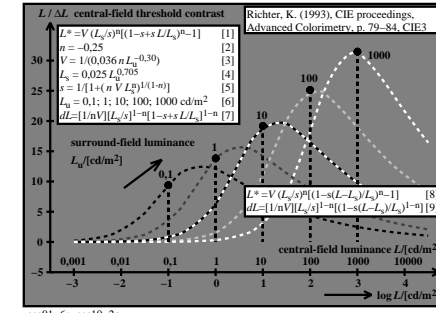
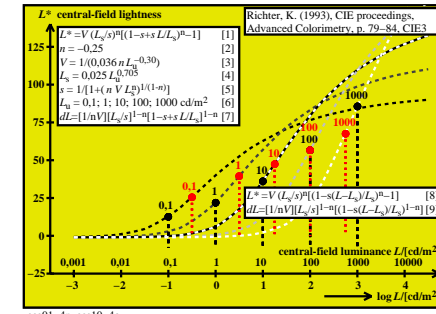
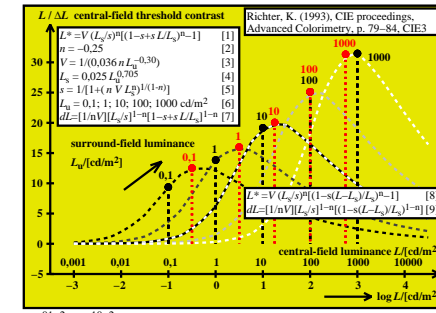
Line-element equations: loudness – sound level¹⁾
 Simple equation by the **Weber-Fechner law** between the loudness N^* and the sound level E
 $\frac{\Delta N^*}{N^*} = n \frac{\Delta E}{E}$ (1)
 It is assumed that at the hearing threshold E_s
 $\frac{\Delta N^*}{N^* + E_s} = n \frac{\Delta E}{E + E_s}$ (2)
 Integration on both sides and requirement $N^* = 0$ for $E = 0$
 $N^* = N^*_s [(1 + \frac{E}{E_s})^n - 1]$ (3)
 Small change with threshold factor s and $N^* = 0$ for $E = E_s$
 $N^* = N^*_s [(1 + s \frac{E-E_s}{E_s})^n - 1]$ (4)

Line-element equations: lightness – tristimulus value
 Richter¹⁾ has used the following equation to approximate between the lightness L^* and the tristimulus value Y
 $L^* = L^*_s [(1 + s \frac{Y-Y_s}{L_s})^n - 1]$ (1)
 The parameters are for the **Munsell Value function**²⁾
 $L^* = 2,5125 s = 0,4250$ $Y_s = 0,1551$ $n = 0,3333$ (2)
 The parameters are for the **CIELAB-lightness function**³⁾
 $L^* = 116 (Y/Y_n)^{1/3} - 16$ ($0,8 < Y < 100$, $Y_n = 100$) (3)
 $L^* = 2,5125 s = 0,4250$ $Y_s = 0,1551$ $n = 0,3333$ (4)

1) Richter, Klaus, (1969), Antagonistic signals in colour vision and relation with the perceived colour order (in German), Dis. Universität Basel, 150 pages, see 115-123, ces00-8N
 2) Newhall, S.M., Nickerson, D., Judd, D.B. (1943), Final report of the O.S.A. subcommittee on the spacing of Munsell Colors, GSA 33, 383-418, see p. 417
 3) ISO/CIE 11664-4:2019 Colorimetry, CIE 1976 $L^*a^*b^*$ colour space
 ces00-8N



ces01-7n, ces10-3a



ces01-8n, ces10-4a

TUB-test chart es0; Achromatic thresholds; 5 luminances $L_u = 0,1, 1, 10, 100, 1000 \text{ cd/m}^2$
 ΔL (0,4s), contrast, and lightness; experimental data of *Lingelbach* and equations of *Richter*

see similar files of the whole serie: <http://farbe.li.tu-berlin.de/ees.htm>
 technical information: <http://farbe.li.tu-berlin.de> OR <http://color.li.tu-berlin.de>