

Line element of Stiles (1946)  
with „cone values“  $L, M, S$   
separate colour response functions

$$F(L) = i \ln(1+9L)$$

$$F(M) = j \ln(1+9M)$$

$$F(S) = k \ln(1+9S)$$

Taylor-derivations:

$$\Delta F(L, M, S) = \frac{dF}{dL} \Delta L + \frac{dF}{dM} \Delta M + \frac{dF}{dS} \Delta S$$

$$= \frac{9i}{1+9L} \Delta L + \frac{9j}{1+9M} \Delta M + \frac{9k}{1+9S} \Delta S$$

feb20-1N

Line element of Vos & Walraven (1972)  
with „cone values“  $L, M, S$   
separate colour response functions

$$F(L) = -2i\sqrt{L}$$

$$F(M) = -2j\sqrt{M}$$

$$F(S) = -2k\sqrt{S}$$

Taylor-derivations:

$$\Delta F(L, M, S) = \frac{dF}{dL} \Delta L + \frac{dF}{dM} \Delta M + \frac{dF}{dS} \Delta S$$

$$\Delta F(L, M, S) = \frac{i}{\sqrt{L}} \Delta L + \frac{j}{\sqrt{M}} \Delta M + \frac{k}{\sqrt{S}} \Delta S$$

feb20-2N

**functions  $q[k(x-u)]$**   
**„achromatic signal“-description**

with  $x = \log L$  ( $L$  = luminance)  
 $u = \log L_u$  ( $L_u$  = surround luminan.)

$$q[k(x-u)] = 1 + 1/[1 + \sqrt{2}e^{k(x-u)}]$$

**function values:**

$$q[k(x-u) \rightarrow +\infty] = 1$$

$$q[k(x-u) = 0] = \sqrt{2}$$

$$q[k(x-u) \rightarrow -\infty] = 2$$

feb20-3N

**„achromatic signal“-description**  
**functions  $Q_{lm}[k(x-u)]$**

with  $x = \log L$  ( $L$  = luminance)  
 $u = \log L_u$  ( $L_u$  = surround luminan.)

$$Q_{lm}[k(x-u)] = \frac{l}{\ln \sqrt{2}} \ln q[k(x-u)] - m$$

**function values with  $l = m = 1$ :**

$$Q[k(x-u) \rightarrow +\infty] = 1$$

$$Q[k(x-u) = 0] = 0$$

$$Q[k(x-u) \rightarrow -\infty] = -1$$

feb20-4N

**„achromatic signal“-discrimination**  
**as function of relative light density**  
 $h = \ln H = k(x-u)$   $\ln$  = natural log.

$$Q' = \frac{d}{dH} [\ln\{1 + 1/(1 + \sqrt{2}H)\}] / \ln \sqrt{2}$$

$$= -\sqrt{2} / [\ln \sqrt{2} (1 + \sqrt{2}H)(2 + \sqrt{2}H)]$$

**function values:**

$$Q'[k(x-u) \rightarrow +\infty] = 0$$

$$Q'[k(x-u) = 0] = -0,5$$

$$Q'[k(x-u) \rightarrow -\infty] = 0$$

feb20-5N

**luminance discrimination**  
**possibility  $L/\Delta L$  as function of  $H$**

with:  $L = 10^x$   $H = e^h = 10^{\log e k(x-u)}$   
 $dL/dx = \ln 10 L$   $dH/dx = k H$

it follows:  $L/\Delta L = [kH / (dH \ln 10)]$

$$\frac{L}{\Delta L} = \text{const } H / [(1 + \sqrt{2}H)(2 + \sqrt{2}H)]$$

$$Q'[k(x-u) \rightarrow +\infty] = 0$$

$$Q'[k(x-u) = 0] = \text{maximum}$$

$$Q'[k(x-u) \rightarrow -\infty] = 0$$

feb20-6N