

Lightness L^*_{JND} for the Just Noticeable Difference (JND)

For adjacent surface colours in the range $3,6 < Y < 90$

or the digital range $100/255 = 0,39 < Y < 100$ it is valid:

$$L^*_{\text{JND}} = a (Y/Y_n)^k \quad [1] \quad a=572; Y_n=100; k=0,14=1/7,2$$

$$= b (Y/Y_u)^k \quad [2] \quad b=a(Y_u/Y_n)^k=450; Y_u=18$$

For $Y=Y_u$ it is valid: $L^*_{\text{JND}_u}=450$.

Derivation of equation [2] gives with $1-k = 0,86$:

$$\delta(L^*_{\text{JND}})/\delta Y = c (Y/Y_u)^{1-k} \quad [3] \quad c = (b k)/Y_u = 63/18 = 3,5$$

or for the treshhold $\delta(L^*_{\text{JND}})=1$

$$\delta Y = d (Y/Y_u)^{1-k} \quad [4] \quad d = Y_u/(b k) = 18/63 = 0,29$$

For the surround lightness $L^*_{\text{JND}_u}=450$ with $Y=Y_u$ the threshold is:

$\delta Y_{\text{JND}_u} = 0,29$. This threshold is *independent* of k .