

Weber-Fechner law in CIE 200-2010 for threshold colour difference of surface colours
 The Weber-Fechner law describes the lightness L^* , as logarithmic function of L . The Stevens law describes the lightness $L_{200,20}^*$ as potential function of L .
 BCC (1992:2) uses a similar potential function: $L_{200,20}^* = a \cdot L^{0.42}$.
 The Weber-Fechner law is equivalent to the equation: $\Delta L_c = c \cdot L$ [1]
 Integration leads to the logarithmic equation: $L^* = k \ln(L)$ [2]
 Differentiation leads to the linear equation: $L_c = k \cdot \Delta L_c$ [3]
 The constant k is called the standard contrast range $\approx 25:100:3.6$.
 Table 1: CIE relative values L^* , luminance L , and lightness L^* .

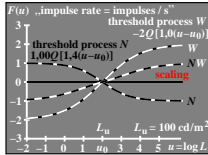
Colour name	Tri-stimulus value	luminance L [cd/m ²]	relative luminance L_c	CIE lightness L^*	relative lightness L^*/L_{100}
constant					
25:100:3.6					
white	0.0408	100	1	100	1
black N	0.0001	0.0001	0.0001	0.0001	0.0001
grey Z (equal)	0.0187	0.0187	0.0187	0.0187	0.0187
grey Y (equal)	0.0187	0.0187	0.0187	0.0187	0.0187
black N	0.0001	0.0001	0.0001	0.0001	0.0001
grey Z (equal)	0.0187	0.0187	0.0187	0.0187	0.0187

For the lightness range between $L^*_0 = 0$ and 40 the constant is: $k = 40 \ln(100)/57$
 CEA5-1N

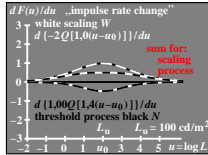
Weber-Fechner law in CIE 200-2010 for threshold colour difference of surface colours and two ranges $0.2 \leq L_c \leq 1$ and $1 \leq L_c \leq 4$
 The Weber-Fechner law describes the lightness L^* , as logarithmic function of L . The Stevens law describes the lightness $L_{200,20}^*$ as potential function of L .
 BCC (1992:2) uses a similar potential function: $L_{200,20}^* = a \cdot L^{0.42}$.
 The Weber-Fechner law is equivalent to the linear equation: $\Delta L_c = c \cdot L$ [1]
 Integration leads to the logarithmic equation: $L^* = k \ln(L)$ [2]
 Differentiation leads to the linear equation: $L_c = k \cdot \Delta L_c$ [3]
 The constant k is called the standard contrast range $\approx 25:100:3.6$.
 Table 2: CIE relative values L^* , luminance L , and lightness L^* .

Colour name	Tri-stimulus value	luminance L [cd/m ²]	relative luminance L_c	CIE lightness L^*	relative lightness L^*/L_{100}
constant					
25:100:3.6					
white	0.0408	100	1	100	1
black N	0.0001	0.0001	0.0001	0.0001	0.0001
grey Z (equal)	0.0187	0.0187	0.0187	0.0187	0.0187
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black N	0.0001	0.0001	0.0001	0.0001	0.0001
grey Z (equal)	0.0187	0.0187	0.0187	0.0187	0.0187

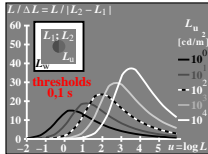
For the two lightness ranges k is $k_{0.2-40} = 42 \ln(100)/21$ and $k_{1-40} = 40 \ln(100)/57$.
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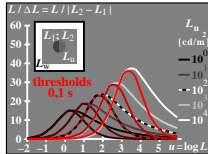
CEA5-1N



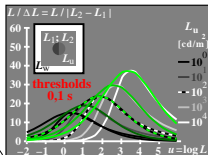
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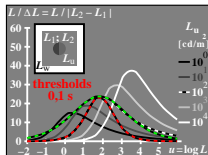
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line element of Stiles (1946) with „color values“ L_P, M_D, S_T
 three separate color signal functions
 $F(L_P) = i \ln(1 + 9 L_P)$
 $F(M_D) = j \ln(1 + 9 M_D)$
 $F(S_T) = k \ln(1 + 9 S_T)$

Taylor-derivations:
 $\Delta F(L_P, M_D, S_T) = \frac{dF}{dL_P} \Delta L_P + \frac{dF}{dM_D} \Delta M_D + \frac{dF}{dS_T} \Delta S_T$
 $= \frac{9i}{1+9L_P} \Delta L_P + \frac{9j}{1+9M_D} \Delta M_D + \frac{9k}{1+9S_T} \Delta S_T$

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line element of Vos&Walraven (1972) with „color values“ L_P, M_D, S_T
 three separate color signal functions
 $F(L_P) = -2i \sqrt{L_P}$
 $F(M_D) = -2j \sqrt{M_D}$
 $F(S_T) = -2k \sqrt{S_T}$

Taylor-derivations:
 $\Delta F(L_P, M_D, S_T) = \frac{dF}{dL_P} \Delta L_P + \frac{dF}{dM_D} \Delta M_D + \frac{dF}{dS_T} \Delta S_T$
 $\Delta F(L_P, M_D, S_T) = \frac{i}{\sqrt{L_P}} \Delta L_P + \frac{j}{\sqrt{M_D}} \Delta M_D + \frac{k}{\sqrt{S_T}} \Delta S_T$

CEA5-2N

functions $q[k(u-u_0)]$
 „achromatic signal“-description
 with $u = \log L$ ($L =$ luminance)
 $u_0 = \log L_0$ ($L_0 =$ surround luminance)
 $q[k(u-u_0)] = 1 + 1/[1 + \sqrt{2} e^{k(u-u_0)}]$
function values:
 $q[k(u-u_0) \rightarrow +\infty] = 1$
 $q[k(u-u_0) = 0] = \sqrt{2}$
 $q[k(u-u_0) \rightarrow -\infty] = 2$

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„achromatic signal“-description functions $Q_{lm}[k(u-u_0)]$
 with $u = \log L$ ($L =$ luminance)
 $u_0 = \log L_0$ ($L_0 =$ surround luminance)
 $Q_{lm}[k(u-u_0)] = \frac{l}{\ln \sqrt{2}} \ln q[k(u-u_0)] - m$
function values with $l = m = 1$:
 $Q[k(u-u_0) \rightarrow +\infty] = -1$
 $Q[k(u-u_0) = 0] = 0$
 $Q[k(u-u_0) \rightarrow -\infty] = 1$

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„achromatic signal“ discrimination as function of relative light density
 $h = \ln H = k(u-u_0)$, $\ln =$ natural log.
 $Q' = \frac{d}{dh} [1/(1+(1+\sqrt{2}H))] / \ln \sqrt{2}$
 $= -\sqrt{2}/(\ln \sqrt{2} (1+\sqrt{2}H)(2+\sqrt{2}H))$
function values:
 $Q'[k(u-u_0) \rightarrow +\infty] = 0$
 $Q'[k(u-u_0) = 0] = -0,5$
 $Q'[k(u-u_0) \rightarrow -\infty] = 0$

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luminance discrimination possibility $L/\Delta L$ as function of H
 with: $L = 10^u$, $H = e^{-k} = 10^{-\log e k(u-u_0)}$
 $dL/dL = \ln 10 L$, $dH/dH = k H$
 l follows: $L/\Delta L = [k H / (dH \ln 10)]$
 $\frac{L}{\Delta L} = \text{const } H / ((1+\sqrt{2}H)(2+\sqrt{2}H))$
function values:
 $Q'[k(u-u_0) \rightarrow +\infty] = 0$
 $Q'[k(u-u_0) = 0] = \text{maximum}$
 $Q'[k(u-u_0) \rightarrow -\infty] = 0$

CEA5-4N

double line element of Richter (1987) for the lighting technology with the luminance $L = f(L_P, M_D, S_T)$
 $F(L) = \int_{L_0}^L (L/\Delta L) dL$ (relative L, M, S^2)
 $F(L) = i Q(H) = \int i Q(H) (u-u_0)$
 $Q(H) = (\ln(1+1/(1+\sqrt{2}H)))/\ln \sqrt{2} - 1$
 Taylor-derivations:
 $\Delta F(L) = \frac{dF}{dL} \Delta L = i \frac{dQ}{dH} \Delta H$
 $H = e^{k(u-u_0)}$, $\bar{H} = e^{k(u-u_0)}$, $\bar{H} = e^{k(u-u_0)}$

CEA5-2N

double line element of Richter (1987) for the lighting technology with the luminance $L = f(L_P, M_D, S_T)$
 $F(L) = \int_{L_0}^L (L/\Delta L) dL$ (relative L, M, S^2)
 $F(L) = i Q(H) = \int i Q(H) (u-u_0)$
 $Q(H) = (\ln(1+1/(1+\sqrt{2}H)))/\ln \sqrt{2} - 1$
 Taylor-derivations:
 $\Delta F(L) = \frac{dF}{dL} \Delta L = i \frac{dQ}{dH} \Delta H$
 $H = e^{k(u-u_0)}$, $\bar{H} = e^{k(u-u_0)}$, $\bar{H} = e^{k(u-u_0)}$

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see similar files: http://farbe.li.tu-berlin.de/CEA5/CEA5.HTM
 technical information: http://farbe.li.tu-berlin.de or http://130.149.60.45/~farbmetrik

TUB registration: 20201101-CEA5/CEA5L0N1.TXT /PS application for evaluation and measurement of display or print output TUB material: code=thadta