

V L O Y M C -8

<http://farbe.li.tu-berlin.de/iej0/iej0l0np.pdf> /ps; only vector graphic VG; start output see separate images of this page: <http://farbe.li.tu-berlin.de/iej0/iej0.htm>

Line-element examples for grey samples ($0.2 \leq x \leq 5$)

$F(x)$ is called the line-element function of $f(x)$.
The following relations are valid for $x=Y/Y_u=1/18$:

$$\frac{d[F(x)]}{dx} = f(x) \quad [1]$$

$$F(x) = \int \frac{f'(x)}{f(x)} dx \quad [2]$$

Example for the normalized tristimulus value $x=Y/Y_u$:

$$\frac{d/a \ln(1+b x)}{dx} = \frac{ab}{1+bx} \quad [3]$$

$$a \ln(1+b x) = \int \frac{ab}{1+bx} dx \quad [4]$$

iej00-1n HEX00-1N

Line-element examples for grey samples ($0.2 \leq x \leq 5$)

$F_u(x)$ is called the line-element function of $f_u(x)$.
Both functions are normalized to the surround value:

$$\frac{d[F_u(x)]}{dx} = f_u(x) \quad [1]$$

$$F_u(x) = \int \frac{f'_u(x)}{f_u(x)} dx \quad [2]$$

Example for the normalized functions with $x_u=1$:

$$F_u(x) = \frac{F(x)}{F(x_u)} = \frac{\ln(1+bx)}{\ln(1+b)} \quad [3]$$

$$f_u(x) = \frac{f(x)}{f(x_u)} = \frac{1+bx}{1+b} \quad [4]$$

iej00-2n HEX00-2N

Line-element examples for grey samples ($0.2 \leq Y_r \leq 5$)

$F(Y_r)$ is called the line-element function of $f(Y_r)$.
The following relations are valid for $Y_r=Y/Y_u=1/18$:

$$\frac{d[F(Y_r)]}{dY_r} = f(Y_r) \quad [1]$$

$$F(Y_r) = \int \frac{f'_u(Y_r)}{f_u(Y_r)} dY_r \quad [2]$$

Example for the normalized tristimulus value $Y_r=Y/Y_u$:

$$\frac{d/a \ln(1+b Y_r)}{dY_r} = \frac{ab}{1+b Y_r} \quad [3]$$

$$a \ln(1+b Y_r) = \int \frac{ab}{1+b Y_r} dY_r \quad [4]$$

iej01-1n HEX01-1N

Line-element examples for grey samples ($0.2 \leq Y_r \leq 5$)

$F_u(Y_r)$ is called the line-element function of $f_u(Y_r)$.
Both functions are normalized to the surround value:

$$\frac{d[F_u(Y_r)]}{dY_r} = f_u(Y_r) \quad [1]$$

$$F_u(Y_r) = \int \frac{f'_u(Y_r)}{f_u(Y_r)} dY_r \quad [2]$$

Example for the normalized functions with $Y_r=1$:

$$F_u(Y_r) = \frac{F(Y_r)}{F(I)} = \frac{\ln(1+b Y_r)}{\ln(1+b)} \quad [3]$$

$$f_u(Y_r) = \frac{f(Y_r)}{f(I)} = \frac{1+b Y_r}{1+b} \quad [4]$$

iej01-2n HEX01-2N

Line-element equations according to CIE 230:2019

Colour-threshold (t) function $f_t(x) = \Delta Y_t = \Delta x Y_u$ [0]
 $\Delta Y_t = (A_1 + A_2 Y)/A_0$ $A_0=1.5$, $A_1=0.0170$, $A_2=0.0058$

$$f_u(x) = \frac{\Delta Y_t}{\Delta Y_u} = \frac{1+bx}{1+b} \quad b=A_2 Y_u/A_1 \quad x=Y/Y_u \quad [1]$$

$$F_u(x) = \int \frac{f'_u(x)}{f_u(x)} dx = \int \frac{b}{1+bx} dx \quad [2]$$

Example for $L^*(x)$ & ΔY with $x=Y/Y_u$, $x_u=1$, $b=6,141$:

$$L^*_u(x) = \frac{L^*(x)}{L^*(x_u)} = \frac{\ln(1+bx)}{\ln(1+b)} \quad [3]$$

$$f_u(x) = \frac{\Delta Y_t}{\Delta Y_u} = \frac{1+bx}{1+b} \quad [4]$$

iej00-3n HEX00-3N

Line-element examples for grey samples ($0.2 \leq Y_r \leq 5$)

$F_u(Y_r)$ is called the line-element function of $f_u(Y_r)$.
Both functions are normalized to the surround value:

$$\frac{d[F_u(Y_r)]}{dY_r} = f_u(Y_r) \quad [1]$$

$$F_u(Y_r) = \int \frac{f'_u(Y_r)}{f_u(Y_r)} dY_r = \int \frac{b}{1+b Y_r} dY_r \quad [2]$$

Example for $L^*(Y_r)$ & ΔY_r with $Y_u=1$, $b=6,141$:

$$L^*_u(Y_r) = \frac{L^*(Y_r)}{L^*(Y_u)} = \frac{\ln(1+b Y_r)}{\ln(1+b)} \quad [3]$$

$$f_u(Y_r) = \frac{\Delta Y_t}{\Delta Y_u} = \frac{1+b Y_r}{1+b} \quad [4]$$

iej01-3n HEX01-3N

Line-element equations according to CIE 230:2019

Colour-discrimination function $f(x) = \Delta Y = \Delta x Y_u$ [0]
 $\Delta Y=1/(1+x)(2+x)=1/(1+x)-1/(2+x) \quad x=\sqrt{2} e^{k(u-u_0)}$

$$f_u(x) = \frac{\Delta Y}{\Delta Y_u} = \frac{1+bx}{1+b} - \frac{1+0.5bx}{1+0.5b} \quad b=1, x=Y/Y_u \quad [1]$$

$$F_u(x) = \int \frac{f'_u(x)}{f_u(x)} dx = \int \frac{b}{1+bx} dx - \int \frac{0.5b}{1+0.5bx} dx \quad [2]$$

Example for $L^*(x)$ & ΔY with $x=Y/Y_u$, $x_u=1$, $b=1$:

$$L^*_u(x) = \frac{L^*(x)}{L^*(x_u)} = \frac{\ln(1+bx)}{\ln(1+b)} - \frac{\ln(1+0.5bx)}{\ln(1+0.5b)} \quad [3]$$

$$f_u(x) = \frac{\Delta Y}{\Delta Y_u} = \frac{1+bx}{1+b} - \frac{1+0.5bx}{1+0.5b} \quad [4]$$

see K. Richter (1996), Computer Graphic and Colorimetry, p. 113–127
<http://color.li.tu-berlin.de/BUA4BF.PDF>

iej00-5n HEX00-5N

Line-element equations for thresholds and scaling

Colour-discrimination function $f(x) = \Delta Y = \Delta x Y_u$ [0]
 $\Delta Y=1/(1+x)(2+x)=1/(1+x)-1/(2+x) \quad x=\sqrt{2} e^{k(u-u_0)}$

$$f_u(x) = \frac{\Delta Y}{\Delta Y_u} = \frac{1+bx}{1+b} - \frac{1+0.5bx}{1+0.5b} \quad b=1, x=Y/Y_u \quad [1]$$

$$F_u(x) = \int \frac{f'_u(x)}{f_u(x)} dx = \int \frac{b}{1+bx} dx - \int \frac{0.5b}{1+0.5bx} dx \quad [2]$$

Example for $L^*(x)$ & ΔY with $x=Y/Y_u$, $x_u=1$, $b=1$:

$$L^*_u(x) = \frac{L^*(x)}{L^*(x_u)} = \frac{\ln(1+bx)}{\ln(1+b)} - \frac{\ln(1+0.5bx)}{\ln(1+0.5b)} \quad [3]$$

$$f_u(x) = \frac{\Delta Y}{\Delta Y_u} = \frac{1+bx}{1+b} - \frac{1+0.5bx}{1+0.5b} \quad [4]$$

see K. Richter (1996), Computer Graphic and Colorimetry, p. 113–127
<http://color.li.tu-berlin.de/BUA4BF.PDF>

iej00-6n HEX00-6N

Line-element equations for thresholds and scaling

Colour-discrimination function $f(y) = \Delta Y = \Delta y Y_u$ [0]
 $\Delta Y=1/(y(1+y))=1/y-1/(1+y) \quad y=1+\sqrt{2} e^{k(u-u_0)}$

$$f_u(y) = \frac{\Delta Y}{\Delta Y_u} = \frac{y}{2} - \frac{1+y}{3} \quad y=1+Y/Y_u, dy=dx \quad [1]$$

$$F_u(y) = \int \frac{f'_u(y)}{f_u(y)} dy = \int \frac{1}{y} dy - \int \frac{1}{1+y} dy \quad [2]$$

Example for $L^*(y)$ & ΔY with $y=1+Y/Y_u$, $y_u=2$:

$$L^*_u(y) = \frac{L^*(y)}{L^*(y_u)} = \frac{\ln(y)}{\ln(2)} - \frac{\ln(1+y)}{\ln(3)} \quad [3]$$

$$f_u(y) = \frac{\Delta Y}{\Delta Y_u} = \frac{1-y}{2} - \frac{1+0.5y}{1.5} \quad [4]$$

see K. Richter (1996), Computer Graphic and Colorimetry, p. 113–127
<http://color.li.tu-berlin.de/BUA4BF.PDF>

iej00-7n HEX00-7N

Line-element equations for thresholds and scaling

Colour-discrimination function $f(Y_r) = \Delta Y_r = \Delta y Y_u$ [0]
 $\Delta Y_r=1/(1+Y_r)(2+Y_r)=1/(1+Y_r)-1/(2+Y_r) \quad Y_r=\sqrt{2} e^{ku}$

$$f_u(Y_r) = \frac{\Delta Y_r}{\Delta Y_u} = \frac{1+Y_r}{2} - \frac{2+Y_r}{3} \quad Y_r=Y/Y_u \quad [1]$$

$$F_u(Y_r) = \int \frac{f'_u(Y_r)}{f_u(Y_r)} dY_r = \int \frac{dY_r}{1+Y_r} - \int \frac{dY_r}{2+Y_r} \quad [2]$$

Example for $L^*(Y_r)$ & ΔY_r with $Y_r=Y/Y_u=1$:

$$L^*_u(Y_r) = \frac{L^*(Y_r)}{L^*(Y_u)} = \frac{\ln(1+Y_r)}{\ln(2)} - \frac{\ln(1+0.5Y_r)}{\ln(1.5)} \quad [3]$$

$$f_u(Y_r) = \frac{\Delta Y_r}{\Delta Y_u} = \frac{1+Y_r}{2} - \frac{1+0.5Y_r}{1.5} \quad [4]$$

see K. Richter (1996), Computer Graphic and Colorimetry, p. 113–127
<http://color.li.tu-berlin.de/BUA4BF.PDF>

iej00-8n HEX00-8N

TUB registration: 20250301-iej0/iej0l0np.pdf /ps
application for evaluation and measurement of display or print output

Line-element equations according to CIE 230:2019

Colour-threshold (t) function $f_t(Y_r) = \Delta Y_t = \Delta Y_r Y_u$ [0]
 $\Delta Y_t = (A_1 + A_2 Y_r)/A_0$ $A_0=1.5$, $A_1=0.0170$, $A_2=0.0058$

$$f_u(Y_r) = \frac{\Delta Y_t}{\Delta Y_u} = \frac{1+b Y_r}{1+b} \quad b=A_2 Y_u/A_1 \quad Y_r=Y/Y_u \quad [1]$$

$$F_u(Y_r) = \int \frac{f'_u(Y_r)}{f_u(Y_r)} dY_r = \int \frac{b}{1+b Y_r} dY_r \quad [2]$$

Example for $L^*(Y_r)$, ΔY_t with $Y_u=Y/Y_r=1$, $b=6,141$:

$$L^*_u(Y_r) = \frac{L^*(Y_r)}{L^*(Y_u)} = \frac{\ln(1+b Y_r)}{\ln(1+b)} \quad [3]$$

$$f_u(Y_r) = \frac{\Delta Y_t}{\Delta Y_u} = \frac{1+b Y_r}{1+b} \quad [4]$$

iej01-4n HEX01-4N

Line-element equations according to CIE 230:2019

Colour-discrimination function $f(Y_r) = \Delta Y_r = \Delta y Y_u$ [0]
 $\Delta Y_r=1/(1+Y_r)(2+Y_r)=1/(1+Y_r)-1/(2+Y_r) \quad Y_r=\sqrt{2} e^{ku}$

$$f_u(Y_r) = \frac{\Delta Y_r}{\Delta Y_u} = \frac{1+b Y_r}{1+b} - \frac{1+0.5b Y_r}{1+0.5b} \quad b=1, Y_r=Y/Y_u \quad [1]$$

$$F_u(Y_r) = \int \frac{f'_u(Y_r)}{f_u(Y_r)} dY_r = \int \frac{b}{1+b Y_r} dY_r - \int \frac{0.5b}{1+0.5b Y_r} dY_r \quad [2]$$

Example for $L^*(Y_r)$ & ΔY_r with $Y_r=Y/Y_u=1$, $b=1$:

$$L^*_u(Y_r) = \frac{L^*(Y_r)}{L^*(Y_u)} = \frac{\ln(1+b Y_r)}{\ln(1+b)} - \frac{\ln(1+0.5b Y_r)}{\ln(1+0.5b)} \quad [3]$$

$$f_u(Y_r) = \frac{\Delta Y_r}{\Delta Y_u} = \frac{1+b Y_r}{1+b} - \frac{1+0.5b Y_r}{1+0.5b} \quad [4]$$

see K. Richter (1996), Computer Graphic and Colorimetry, p. 113–127
<http://color.li.tu-berlin.de/BUA4BF.PDF>

iej01-5n HEX01-5N

Line-element equations for thresholds and scaling

Colour-discrimination function $f(Y_r) = \Delta Y_r = \Delta y Y_u$ [0]
 $\Delta Y_r=1/(1+Y_r)(2+Y_r)=1/(1+Y_r)-1/(2+Y_r) \quad Y_r=\sqrt{2} e^{ku}$

$$f_u(Y_r) = \frac{\Delta Y_r}{\Delta Y_u} = \frac{1+b Y_r}{1+b} - \frac{1+0.5b Y_r}{1+0.5b} \quad b=1, Y_r=Y/Y_u \quad [1]$$

$$F_u(Y_r) = \int \frac{f'_u(Y_r)}{f_u(Y_r)} dY_r = \int \frac{b}{1+b Y_r} dY_r - \int \frac{0.5b}{1+0.5b Y_r} dY_r \quad [2]$$

Example for $L^*(Y_r)$ & ΔY_r with $Y_r=Y/Y_u=1$, $b=1$:

$$L^*_u(Y_r) = \frac{L^*(Y_r)}{L^*(Y_u)} = \frac{\ln(1+b Y_r)}{\ln(1+b)} - \frac{\ln(1+0.5b Y_r)}{\ln(1+0.5b)} \quad [3]$$

$$f_u(Y_r) = \frac{\Delta Y_r}{\Delta Y_u} = \frac{1+b Y_r}{1+b} - \frac{1+0.5b Y_r}{1+0.5b} \quad [4]$$

see K. Richter (1996), Computer Graphic and Colorimetry, p. 113–127
<http://color.li.tu-berlin.de/BUA4BF.PDF>

iej01-6n HEX01-6N

Line-element equations for thresholds and scaling

Colour-discrimination function $f(y) = \Delta Y = \Delta y Y_u$ [0]
 $\Delta Y=1/(y(1+y))=1/y-1/(1+y) \quad y=1+\sqrt{2} e^{k(u-u_0)}$

$$f_u(y) = \frac{\Delta Y}{\Delta Y_u} = \frac{y}{2} - \frac{1+y}{3} \quad y=1+Y/Y_u, dy=dx \quad [1]$$

$$F_u(y) = \int \frac{f'_u(y)}{f_u(y)} dy = \int \frac{1}{y} dy - \int \frac{1}{1+y} dy \quad [2]$$

Example for $L^*(y)$ & ΔY with $y=1+Y/Y_u$, $y_u=2$:

$$L^*_u(y) = \frac{L^*(y)}{L^*(y_u)} = \frac{\ln(y)}{\ln(2)} - \frac{\ln(1+y)}{\ln(3)} \quad [3]$$

$$f_u(y) = \frac{\Delta Y}{\Delta Y_u} = \frac{1-y}{2} - \frac{1+0.5y}{1.5} \quad [4]$$

see K. Richter (1996), Computer Graphic and Colorimetry, p. 113–127
<http://color.li.tu-berlin.de/BUA4BF.PDF>

iej01-7n HEX01-7N

TUB material: code=rha4ta

Line-element equations for thresholds and scaling

Colour-discrimination function $f(y) = \Delta Y = \Delta y Y_u$ [0]
 $\Delta Y=1/(y(1+y))=1/y-1/(1+y) \quad y=1+\sqrt{2} e^{k(u-u_0)}$

$$f_u(y) = \frac{\Delta Y}{\Delta Y_u} = \frac{y}{2} - \frac{1+y}{3} \quad y=1+Y/Y_u, dy=dx \quad [1]$$

$$F_u(y) = \int \frac{f'_u(y)}{f_u(y)} dy = \int \frac{1}{y} dy - \int \frac{1}{1+y} dy \quad [2]$$

Example for $L^*(y)$ & ΔY with $y=1+Y/Y_u$, $y_u=2$:

$$L^*_u(y) = \frac{L^*(y)}{L^*(y_u)} = \frac{\ln(y)}{\ln(2)} - \frac{\ln(1+y)}{\ln(3)} \quad [3]$$

$$f_u(y) = \frac{\Delta Y}{\Delta Y_u} = \frac{1-y}{2} - \frac{1+0.5y}{1.5} \quad [4]$$

see K. Richter (1996), Computer Graphic and Colorimetry, p. 113–127
<http://color.li.tu-berlin.de/BUA4BF.PDF>

iej01-8n HEX01-8N